

# Ladder: A Convergence-based Structured DAG Blockchain for High Throughput and Low Latency

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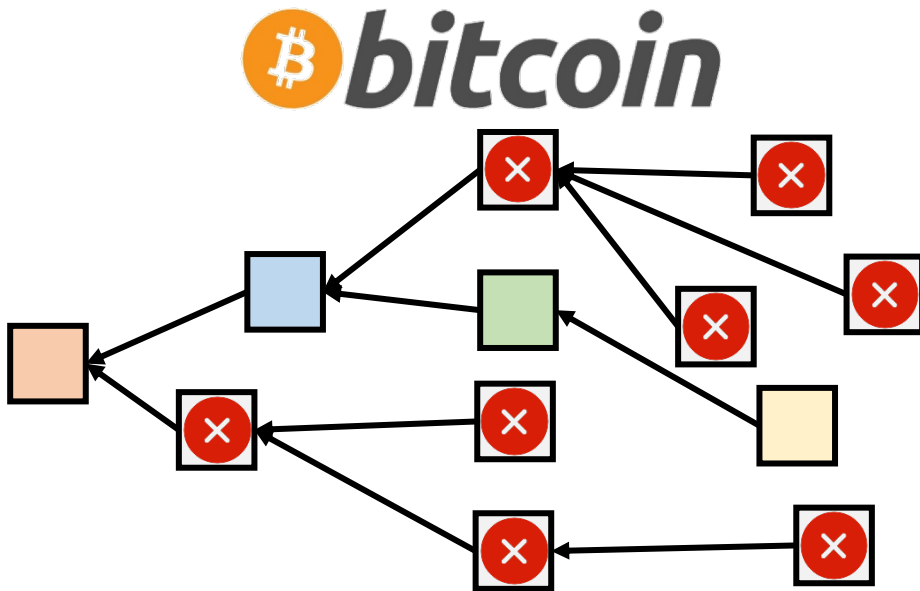
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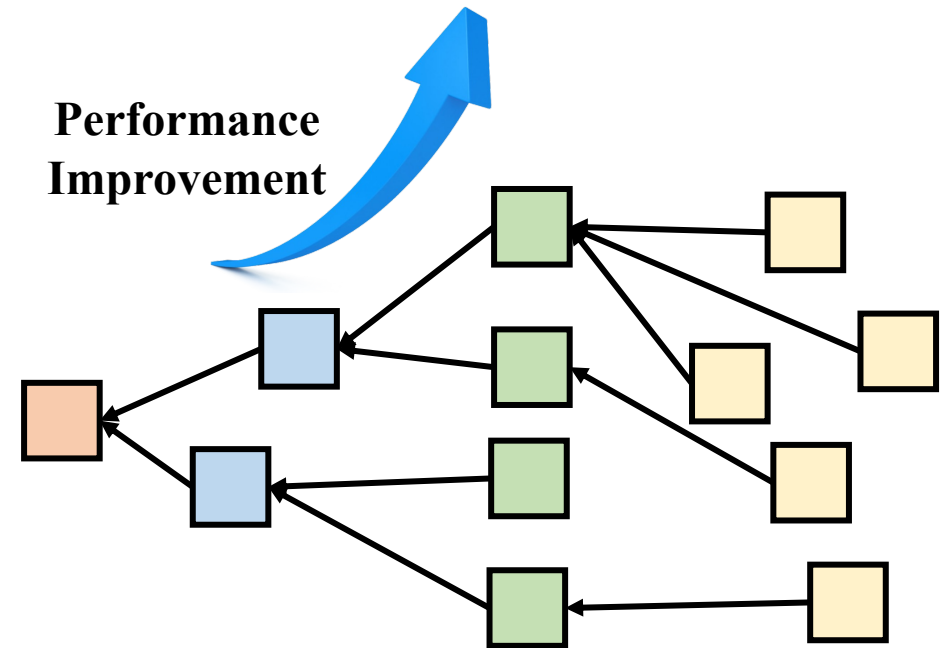
<sup>3</sup>*North Carolina State University*

<sup>4</sup>*Peking University*

**Directed Acyclic Graph (DAG) offers a scalable alternative to chain-style ledgers by enabling concurrent block generation through parallelized topology**

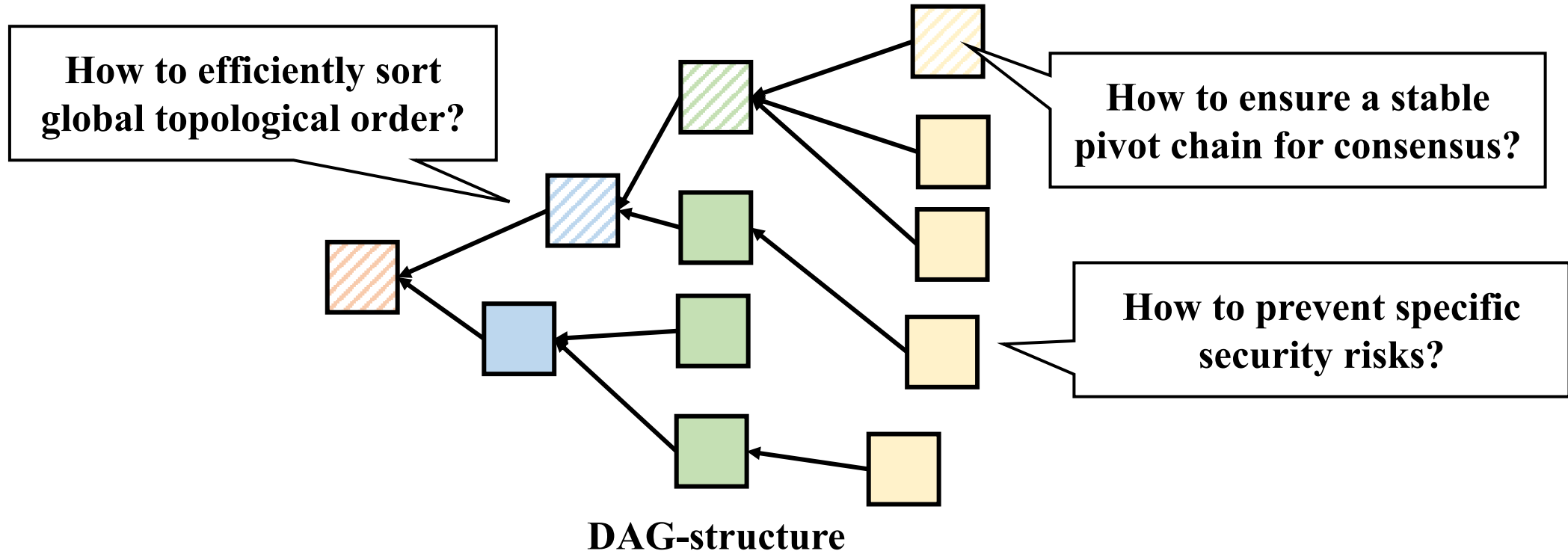


Chain-structure

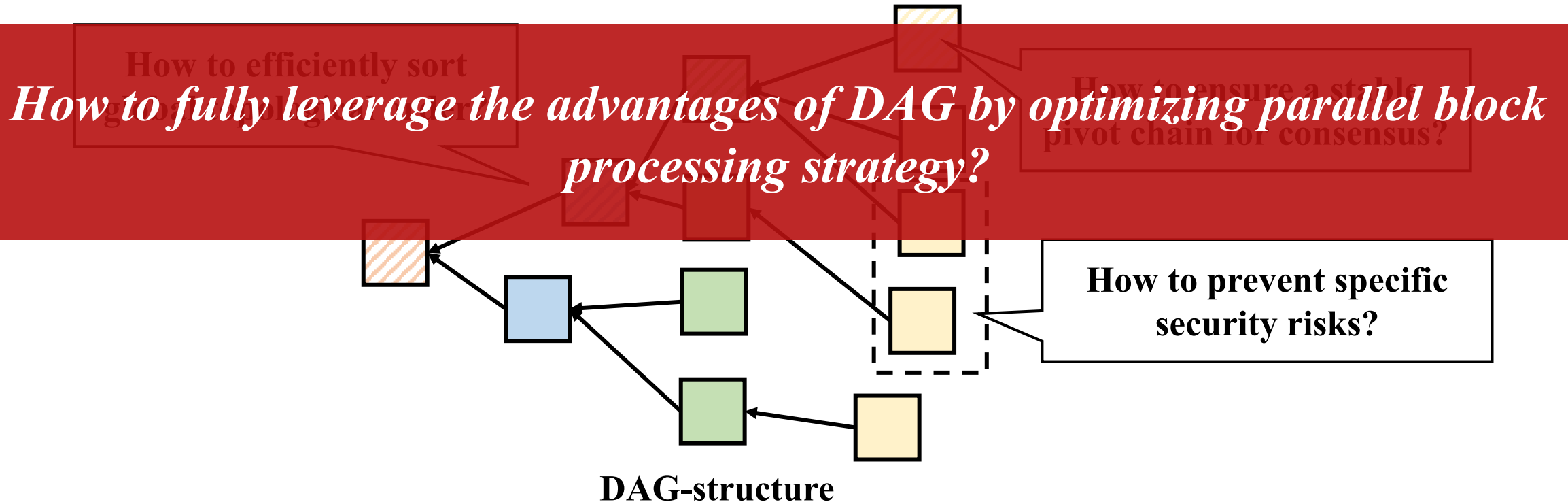


DAG-structure

**Broader DAG structures enhance scalability through parallel block generation but introduce key challenges**

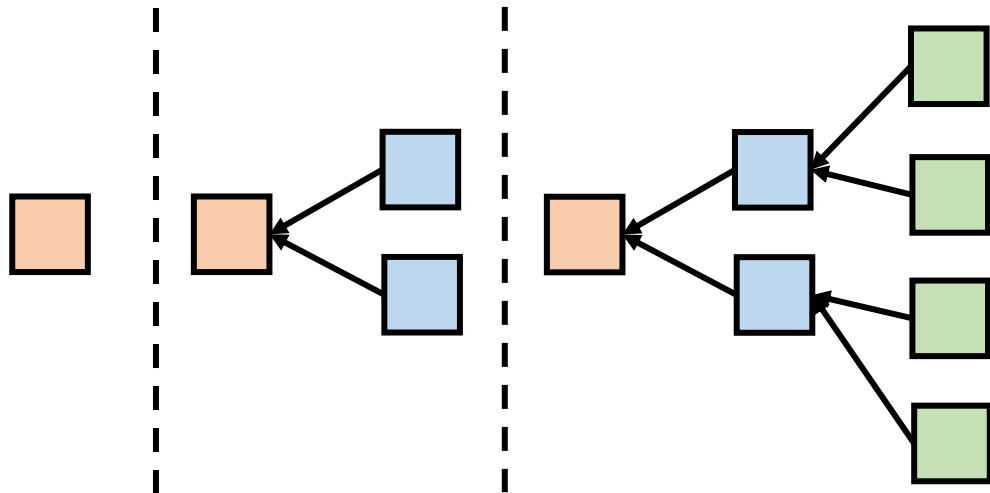


**Broader DAG structures enhance scalability through parallel block generation but introduce key challenges**



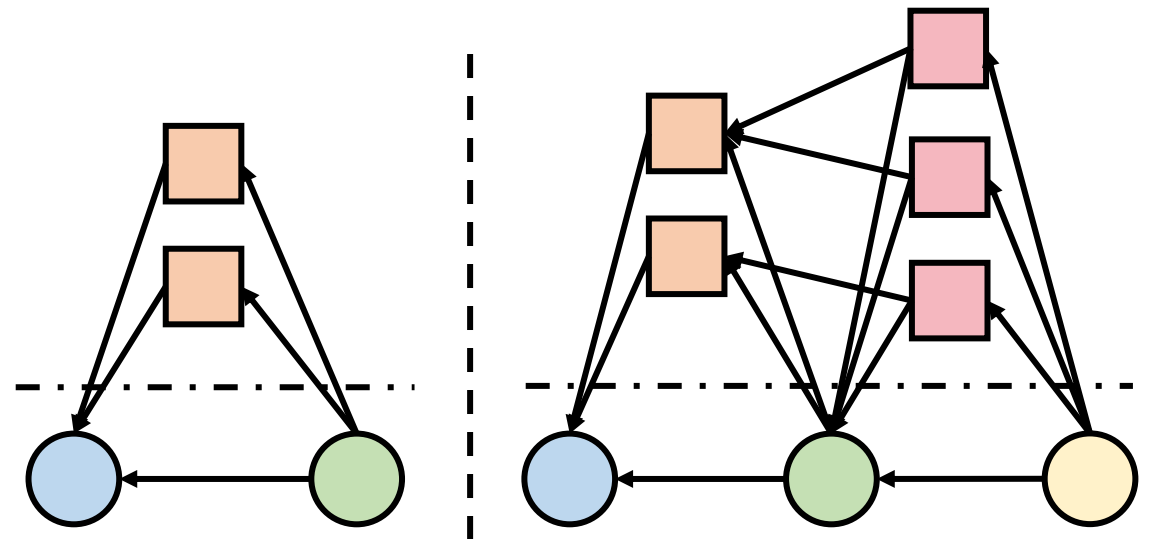
Solutions	Sorting Methods	Confirmation Logic	Balance Attack Resistance	Performance	
				TPS	Latency
GHOST	Independent Local Sorting with Global Confirmation	Reference-count Global Ordering	No	200	<60min
Inclusive		Partially Ordered Ledger	No	350	<1min
Spectre			-	-	<1min
Phantom		Weight-based Global Ordering	No	40	<1min
Conflux			No	2823	<1min
OHIE		Hierarchical Global Ordering	Yes	2513	<10min
Ladder	Single-Node-Driven Ordering & Confirmation		Yes	4506	<1min

Traditional DAG



**Lacking control** over parallel chain topology, leading to **performance limitations** and vulnerability to **balance attacks**.

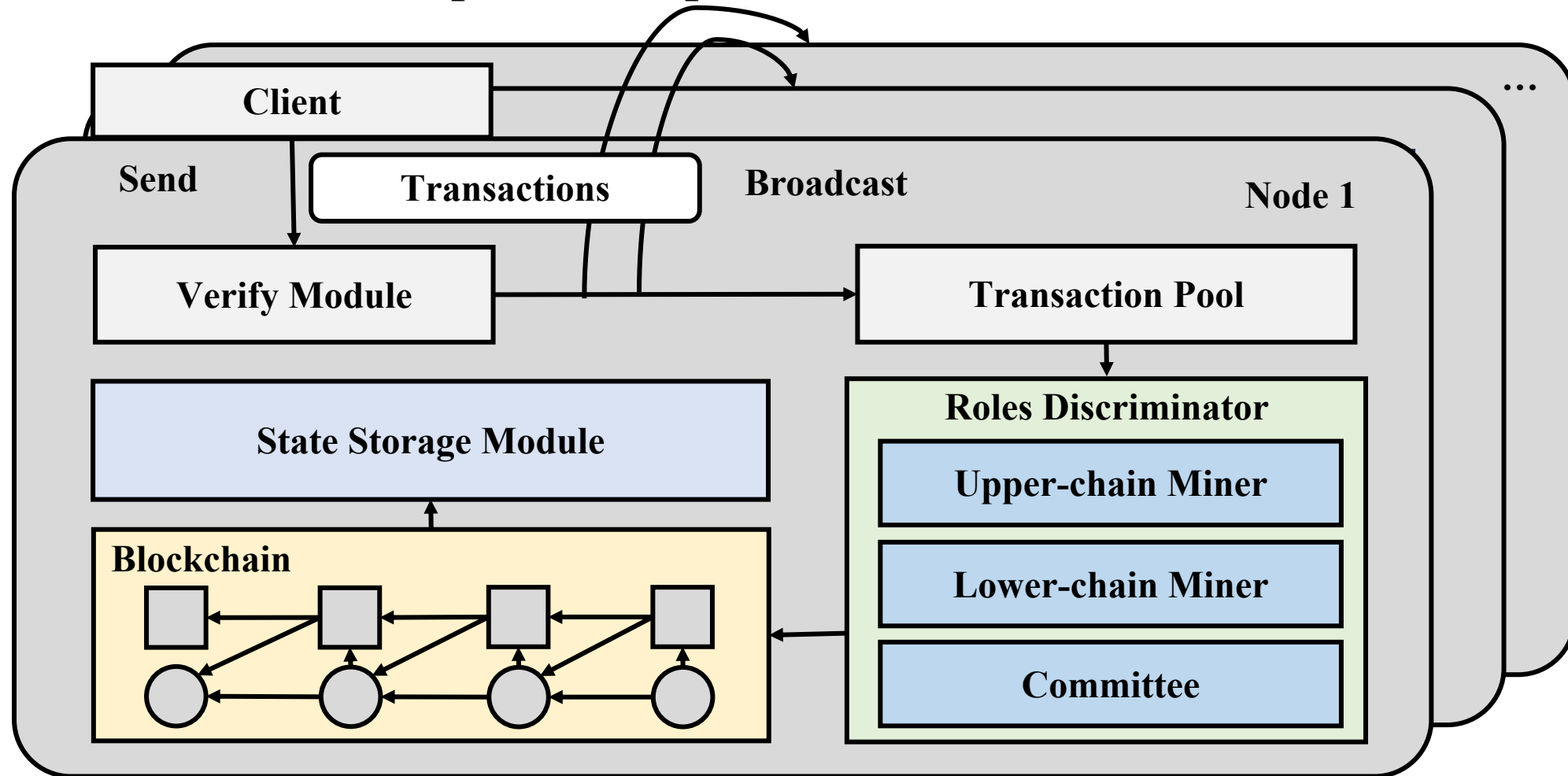
Our Method



Employing a **dual-chain architecture** where one chain structurally constrains the other through **convergent referencing**.

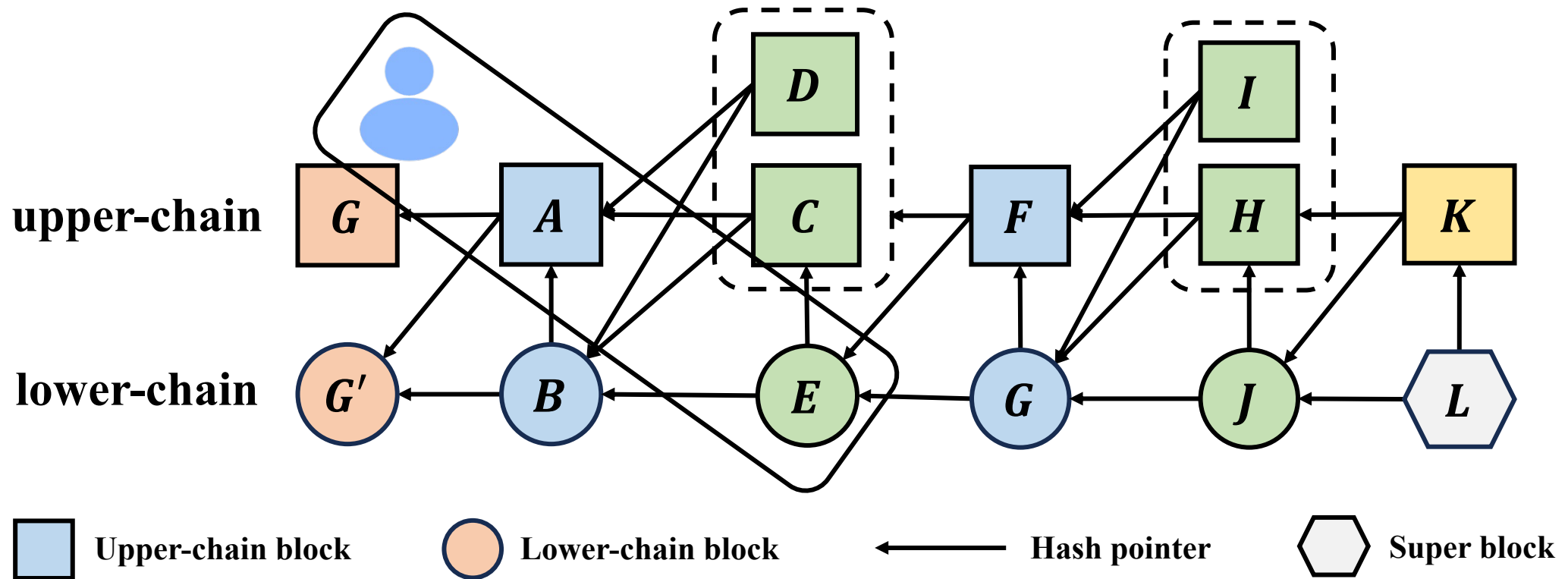
- ❑ *How to use the one-chain to effectively converge generated fork blocks of another chain?*
- ❑ *How to ensure system security by preventing adversaries from becoming convergence nodes?*

Ladder assumes a  $\delta$ -synchronous network and that the adversary contributes less than 30% of the total computational power

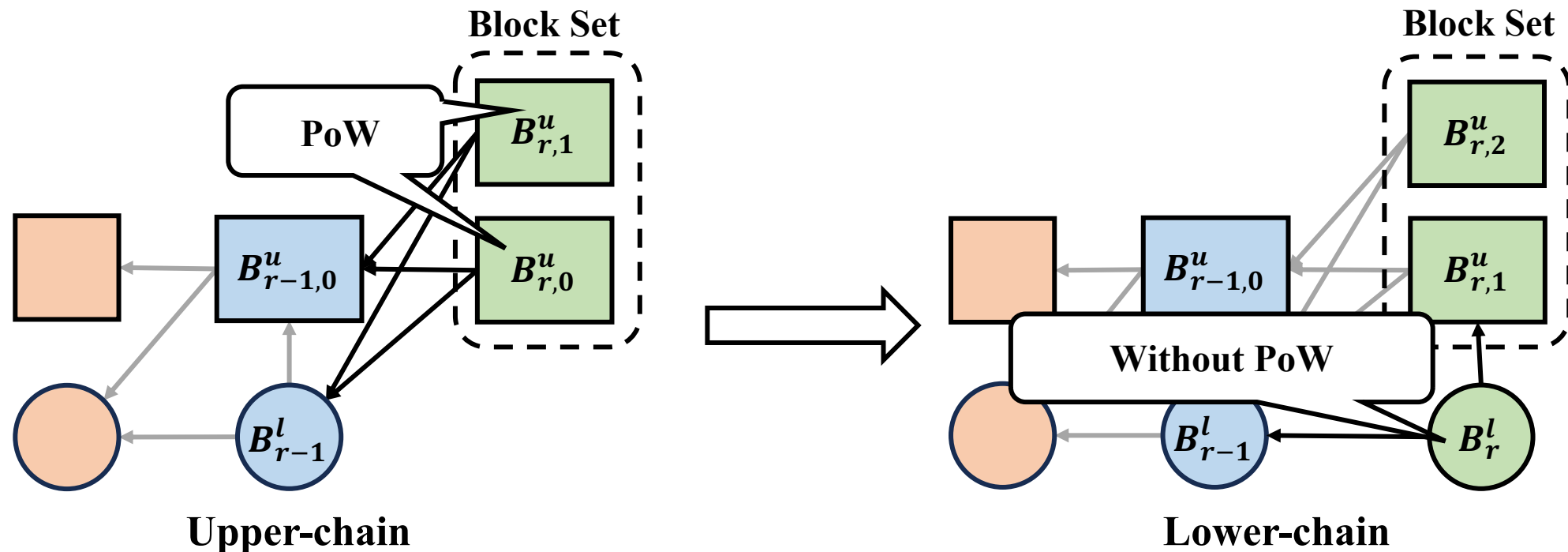




Ladder generates DAG in the upper-chain while the lower-chain drives convergence and narrows the DAG structure



**Nodes in Ladder utilize Proof-of-Work (PoW) for upper-chain block generation while simultaneously regulating the production of lower-chain blocks**



**Ladder uses lower-chain blocks to determine the sequence of all forked upper-chain blocks**

**HCP dynamically weights block subtree difficulty (rather than sub-block count) to select the standard upper-chain blocks**

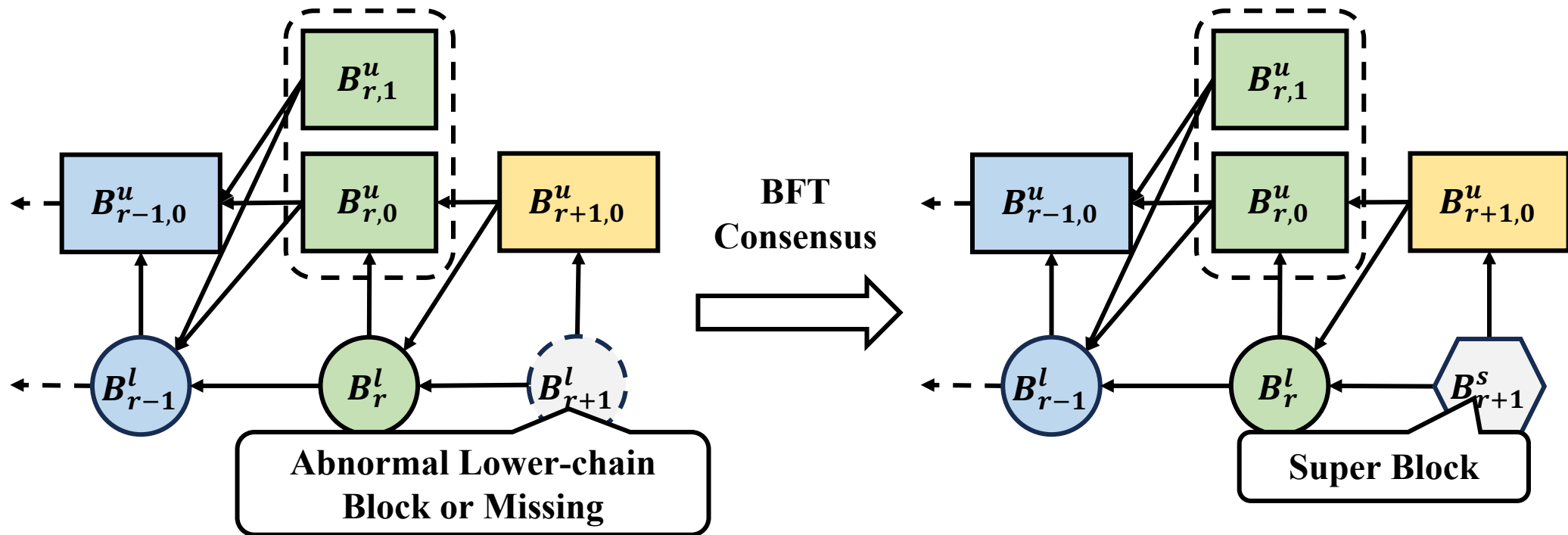
$$\mathcal{D}(B_i) := \sqrt{\mathcal{Z}(B_i)} + \sum_{B_j \in S_i} \mathcal{D}(B_j)$$

The diagram illustrates the formula for block difficulty  $\mathcal{D}(B_i)$ . It consists of three callout boxes with lines pointing to parts of the formula:

- A box on the left points to  $\sqrt{\mathcal{Z}(B_i)}$  and contains the text: "Leading zeros in the hash of block  $B_i$ ".
- A box in the center points to the summation  $\sum_{B_j \in S_i}$  and contains the text: "Set of all legal upper-chain blocks pointing to  $B_i$ ".
- A box on the right points to  $\mathcal{D}(B_j)$  and contains the text: "Difficulty of block  $B_j$ ".

**HCP thwarts liveness and balance attacks by requiring prohibitive computational power to override established subtree weights**

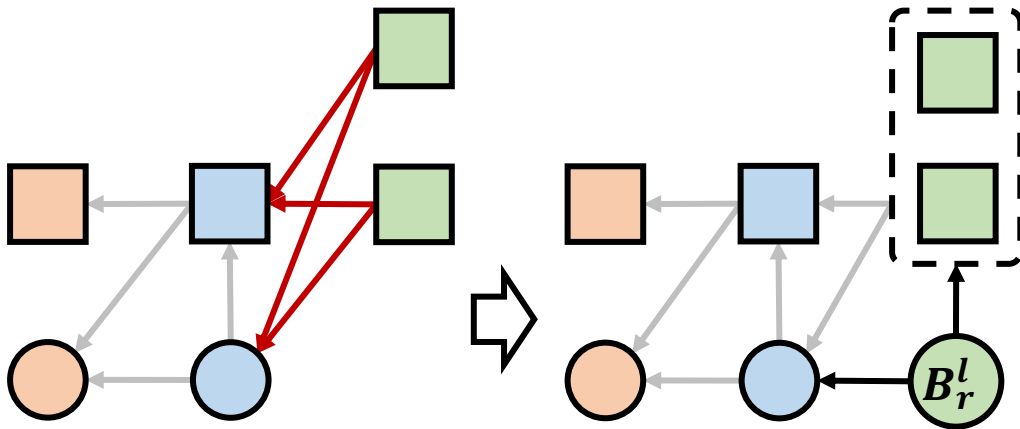
Ladder forms a committee of recent standard upper-chain block producers to generate Super Blocks resolving lower-chain anomalies



Committee employs deterministic BFT consensus to ensure the finality of lower-chain

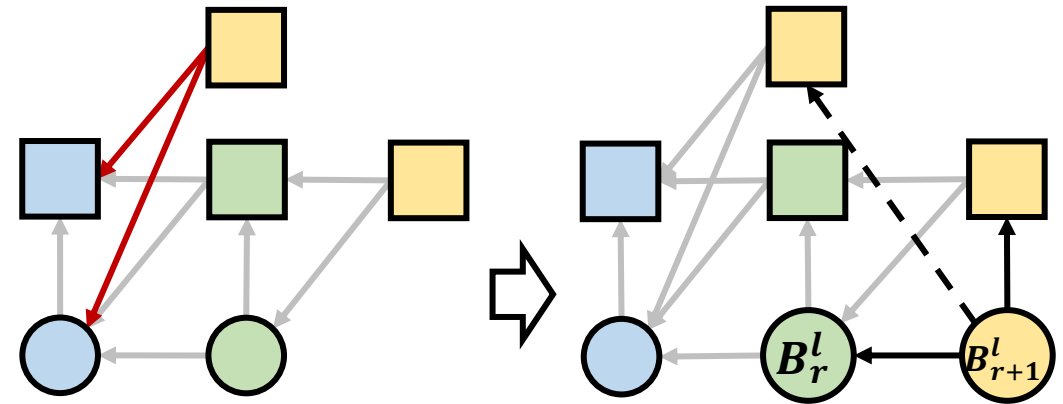
Two upper-chain fork types may occur

Tip Fork



Multiple valid upper-chain blocks in round  $r$ , one block generator is selected by convergence node

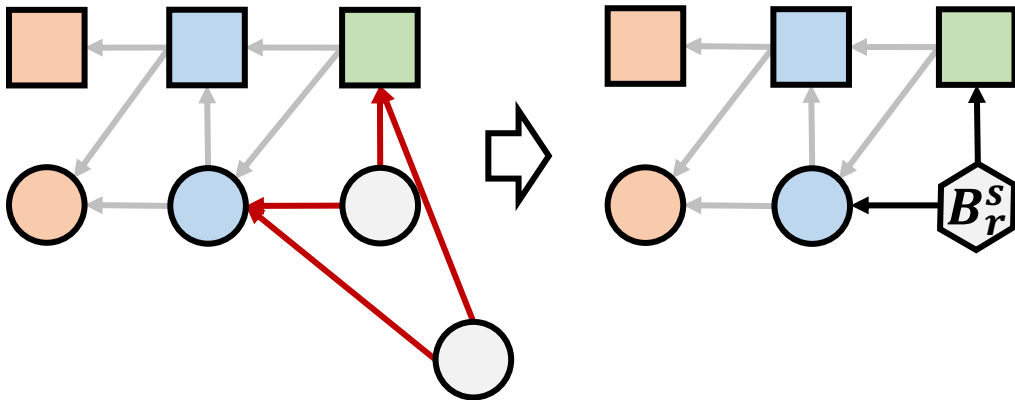
Chain Fork



Delayed upper-chain block in round  $r$ , referenced by lower-chain block in round  $r + 1$

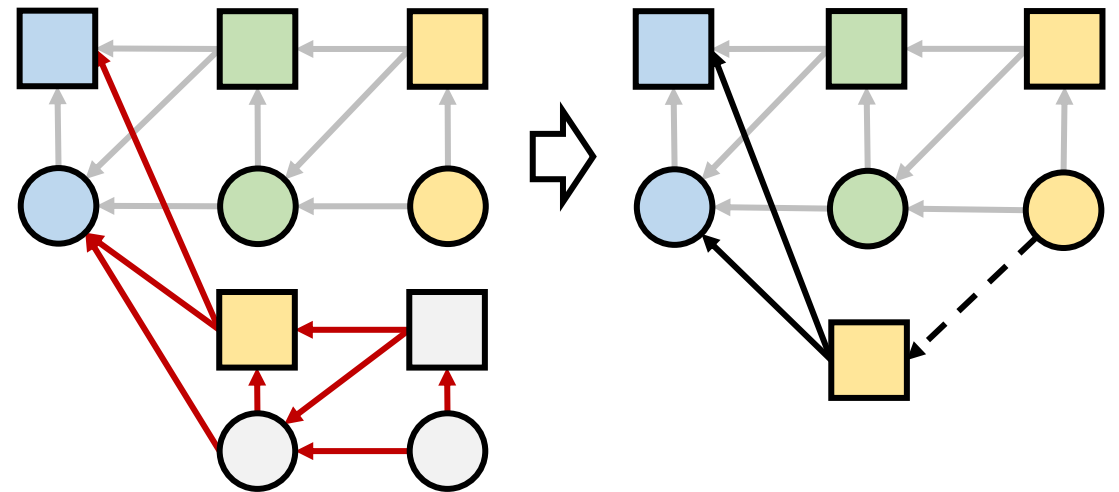
Two lower-chain fork types may occur

Tip Fork



Multiple lower-chain blocks in round  $r$ ,  
resolved by BFT to generate a super block

Chain Fork



Two parallel Ladders may arise, reconciled  
through the Hardest Chain Principle

## BFT Committee Size

- ❑ The BFT committee may introduce security risk: Adversaries exceeding 1/3 when generating the Super Block

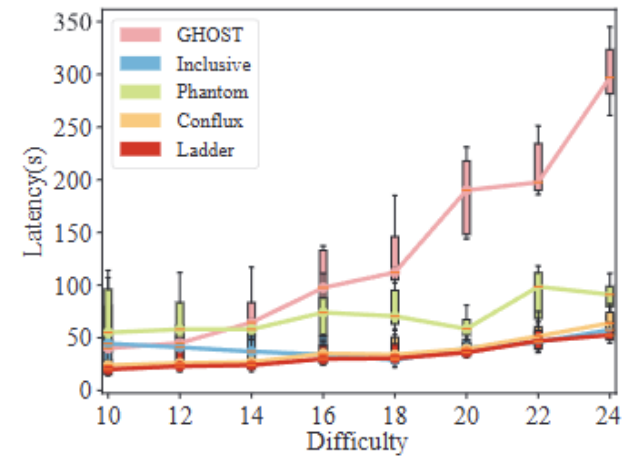
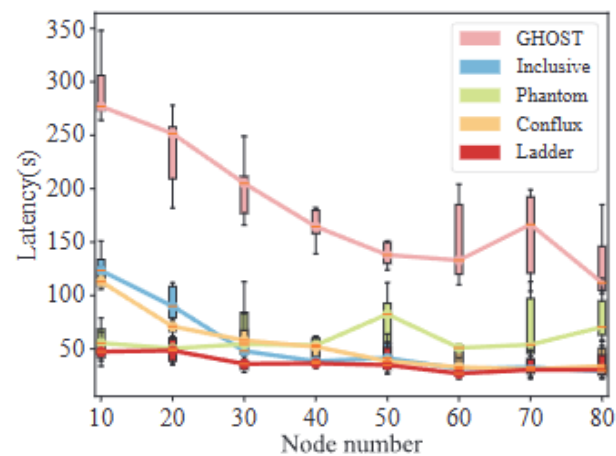
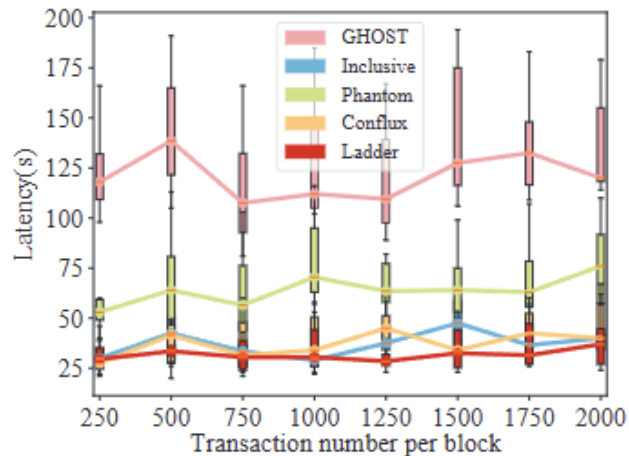
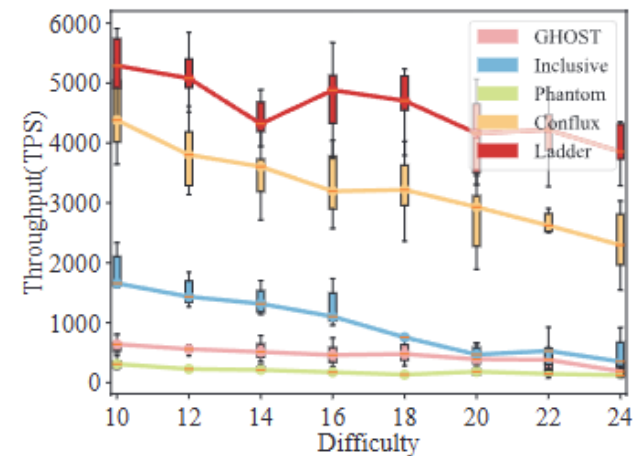
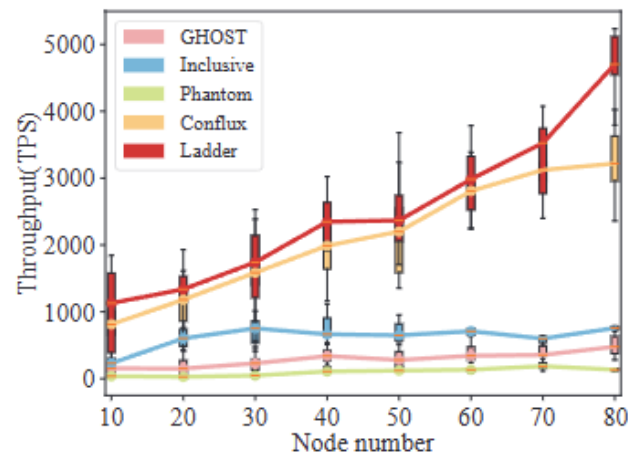
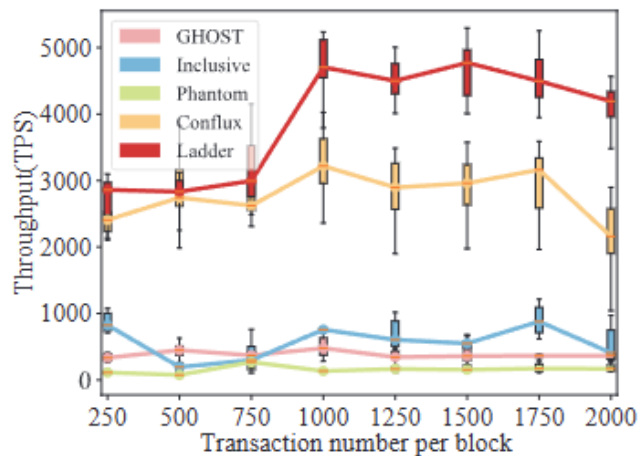
Committee Size	120	180	240	300
Byzantine nodes exceeding 1/3 probability	$4.9 \times 10^{-3}$	$1.8 \times 10^{-4}$	$6 \times 10^{-6}$	$1.96 \times 10^{-7}$
Rounds to reach a cumulative probability of 99%	$9.2 \times 10^2$	$2.6 \times 10^4$	$7.7 \times 10^5$	$2.4 \times 10^7$

**We implement a prototype of Ladder using 80 nodes and compare performance with GHOST, Inclusive, Phantom, and Conflux**

<b>Server</b>	<b>Network Delay</b>	<b>Node Number</b>	<b>PoW Difficulty</b>
<b>Intel(R) Core(TM) i5-4590 CPU@3.30 GHz and 8 GB of RAM</b>	<b>80-120ms</b>	<b>80</b>	<b>18</b>

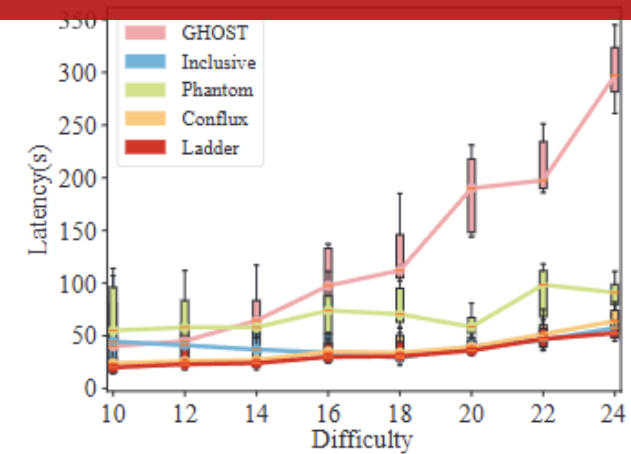
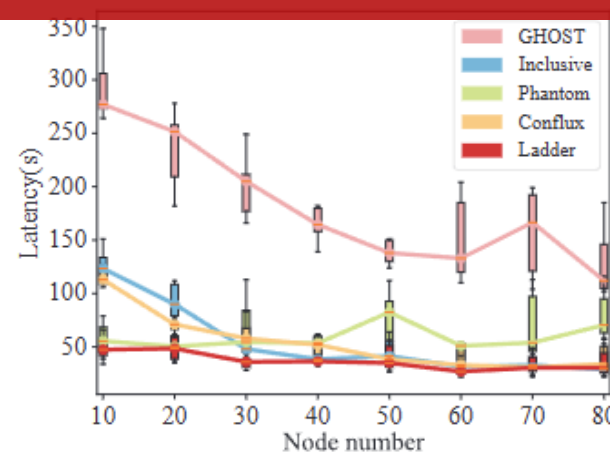
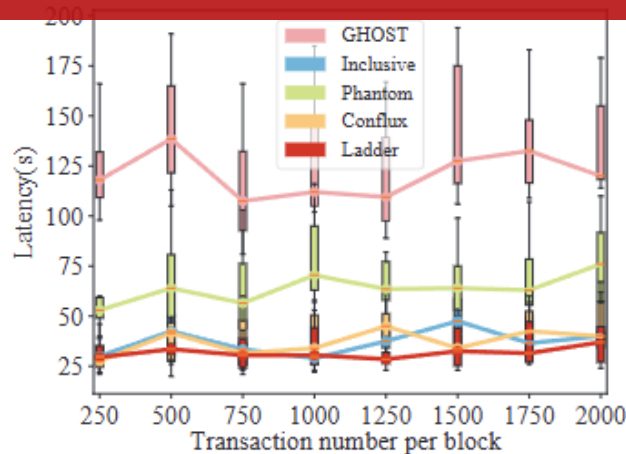
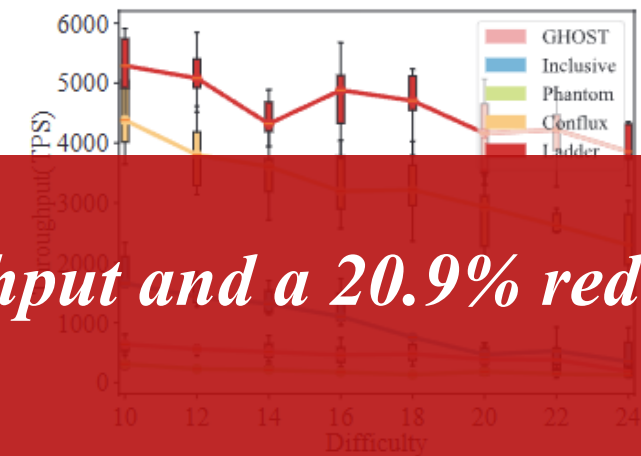
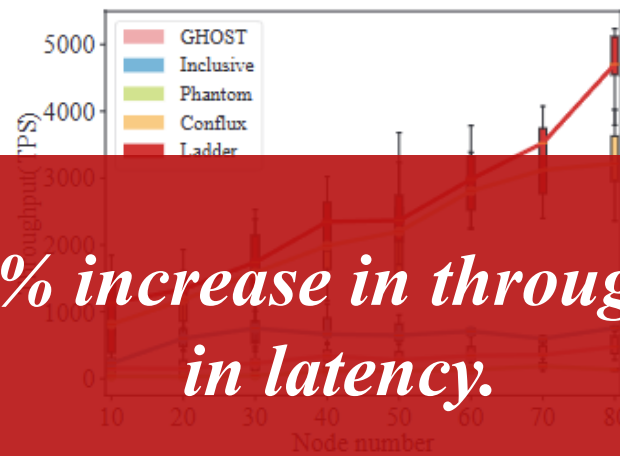
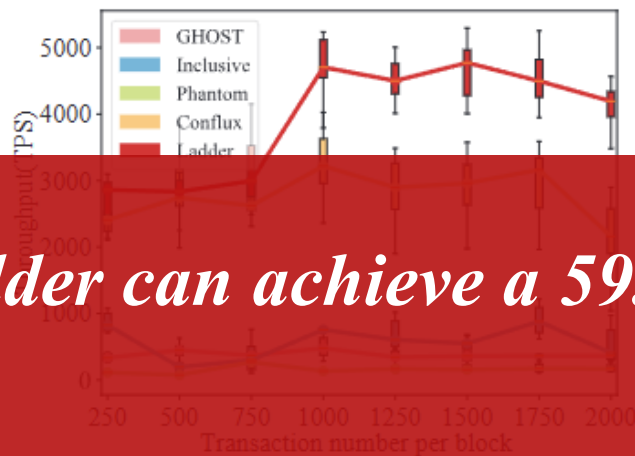


We use three key variables – transaction number per block, node number, and difficulty level – with Throughput and Latency as performance metrics



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*Ladder can achieve a 59.6% increase in throughput and a 20.9% reduction in latency.*



**We make the security analysis from two perspectives:**

**Resistance Against Common Attacks:**

- ❑ Sybil Attack**
- ❑ Denial of Service (DoS) Attack**
- ❑ Double-Spending Attack**
- ❑ Eclipse Attack**

**Security and Availability:**

- ❑ *Theorem 1: Any block in the lower-chain of Ladder is a valid block with a high probability.***
- ❑ *Theorem 2: Ladder satisfies common prefix, finality, and liveness properties.***

# Thanks!

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